

Detecting Chromosomal Inversions from Dense SNPs by Combining PCA and Association Tests

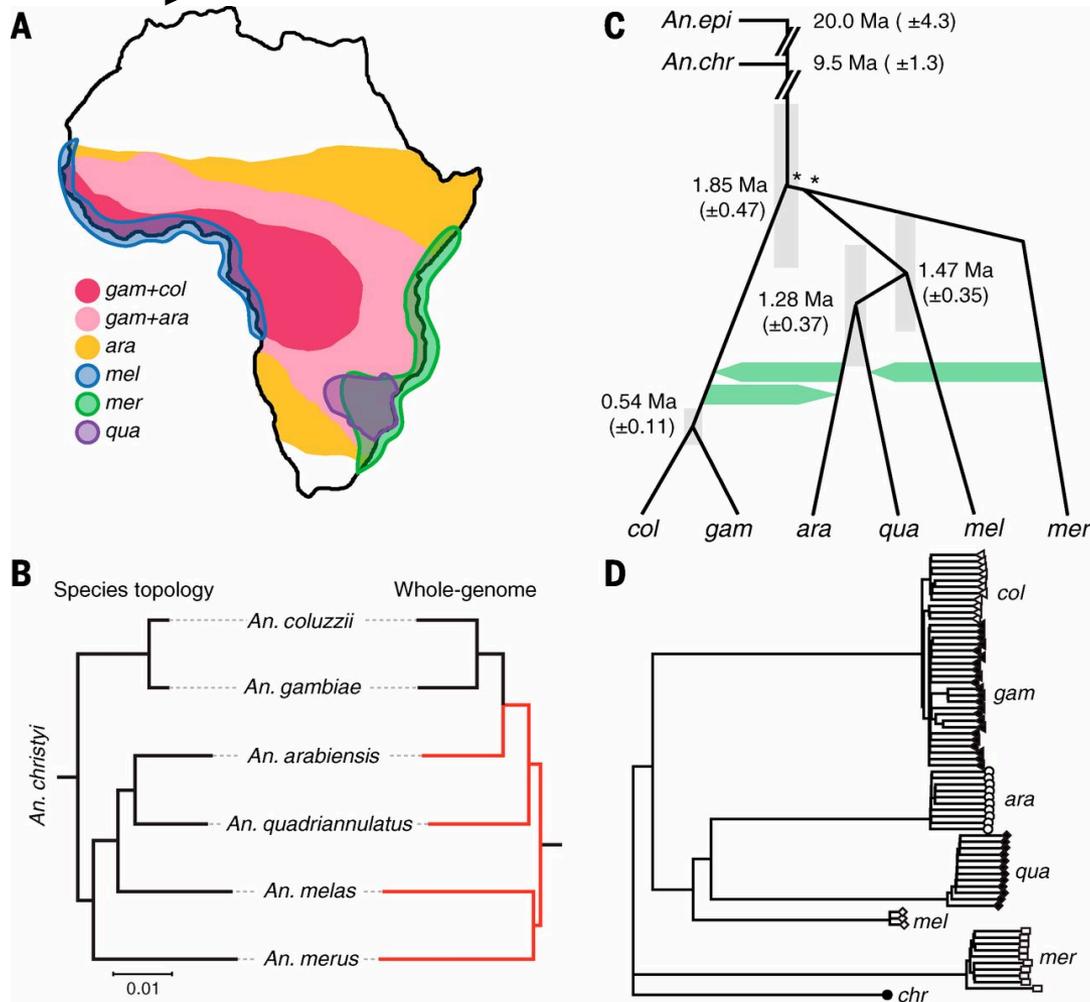
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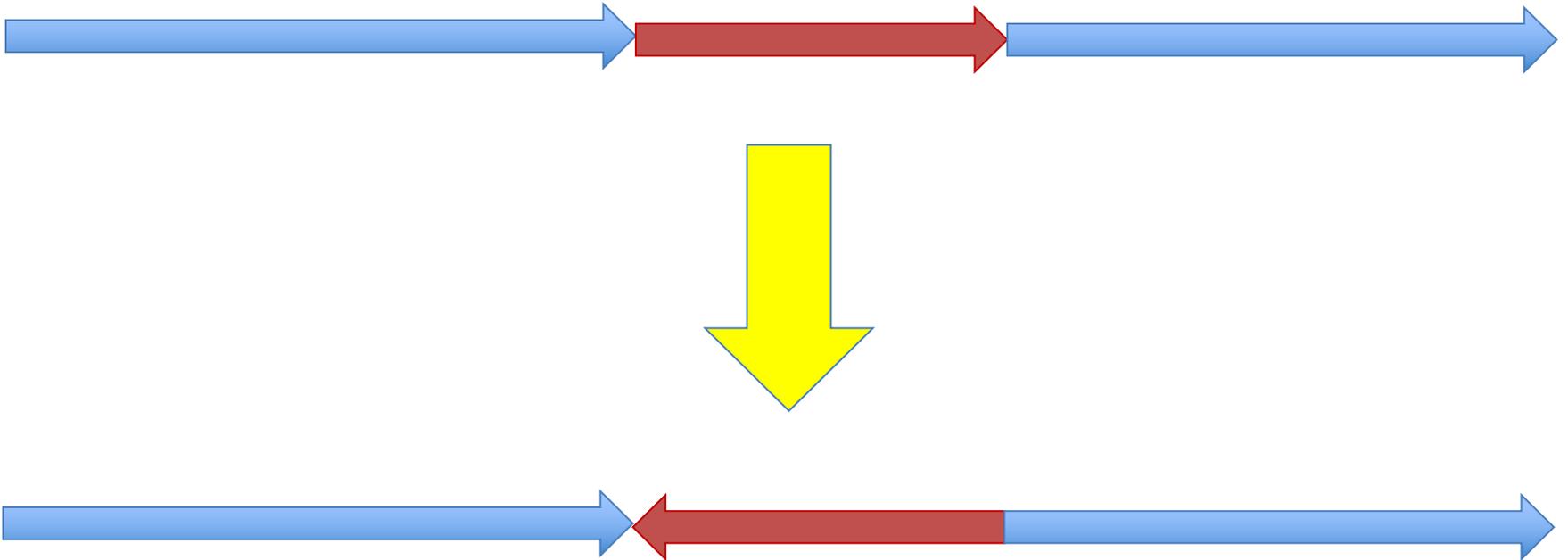
An. gambiae and *An. coluzzii*



Population Genetics



What is an Inversion?



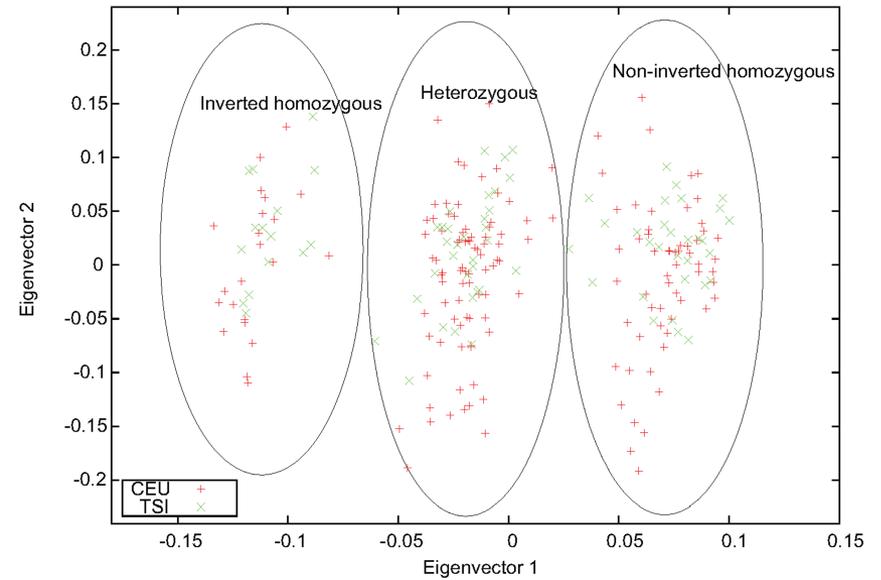
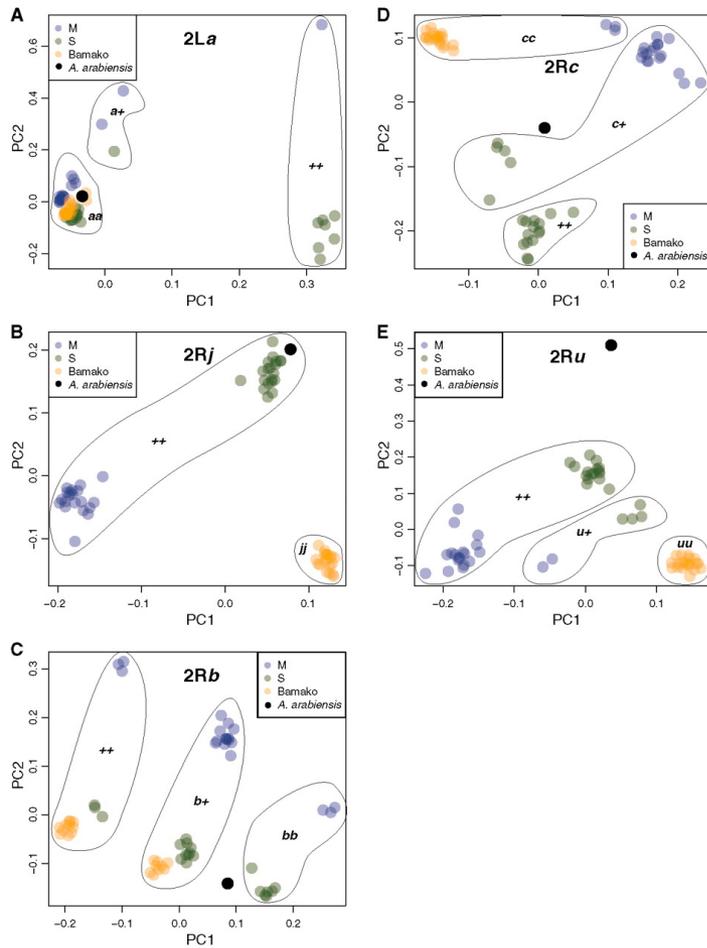
Importance of Inversions

- Thought to play an important role in ecological adaptation by enabling the accumulation of beneficial alleles

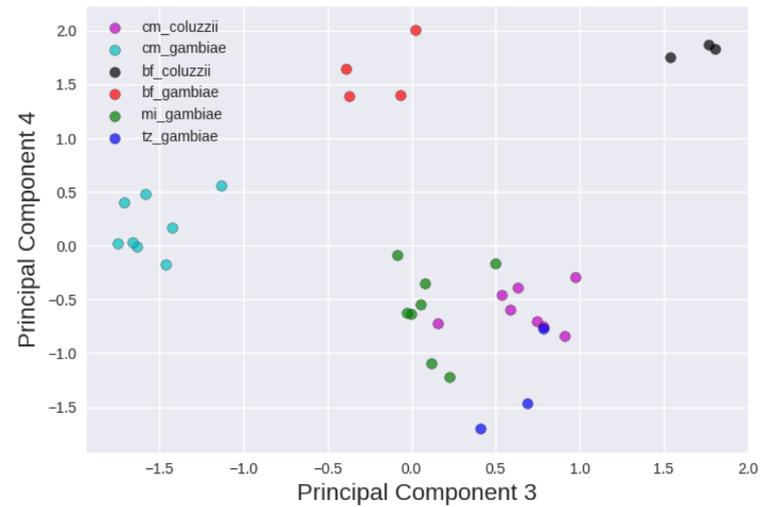
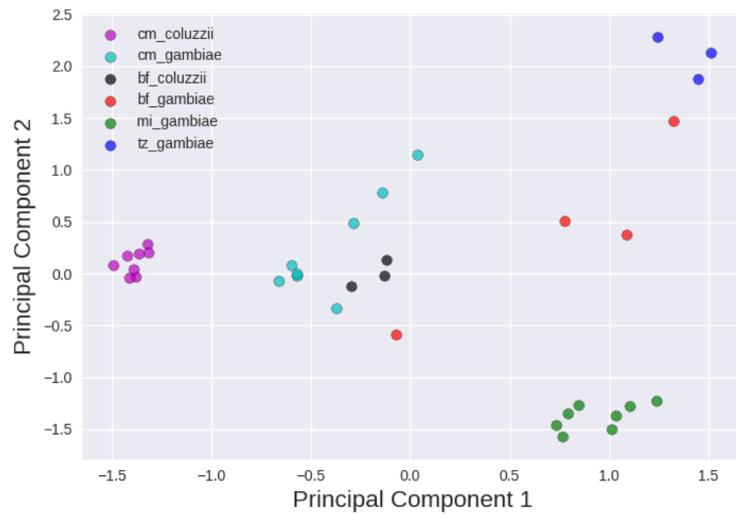
Fuller, et al. *Bioarxiv*. 2017.; Love, et al. *Mol. Ecol.* 2016.

- **2La in *Anopheles gambiae***
 - Thermal tolerance of larvae
Rocca, et al. *Malaria Journal*. 2009.
 - Enhanced desiccation resistance
Gray, et al. *Malaria Journal*. 2009.
 - Susceptibility to malaria parasite species
Riehle, *Elife*. 2016.

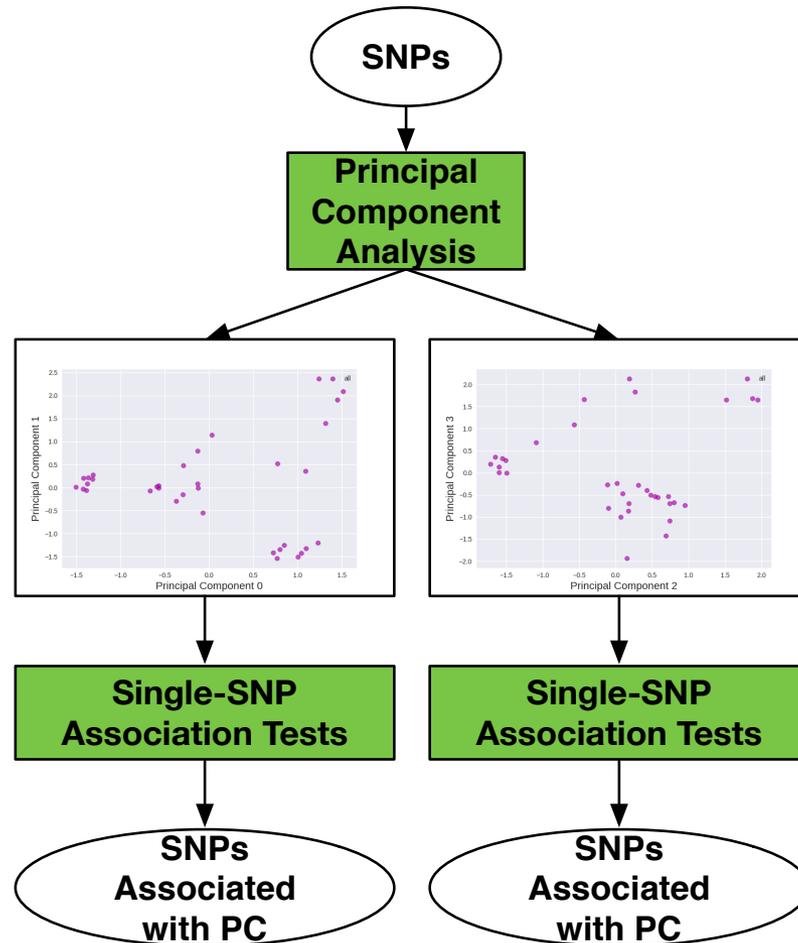
PCA



PCA of Our Samples



Combining PCA and Association Tests



Likelihood-Ratio Test

1. Fit Logistic Regression model

$$P_g(y_{i,g}) = \frac{1}{1 + \exp(-\beta_1 \mathbf{T}_{i,j} + \beta_0)} \quad (1)$$

2. Compute Likelihoods for Null and Alternative Models

$$L(\beta, \beta_0 | \mathbf{T}, \mathbf{y}) = \prod_{i=1}^N \prod_g P(y_{i,g} | \mathbf{T}_{i,j})^{y_{i,g}} \quad (2)$$

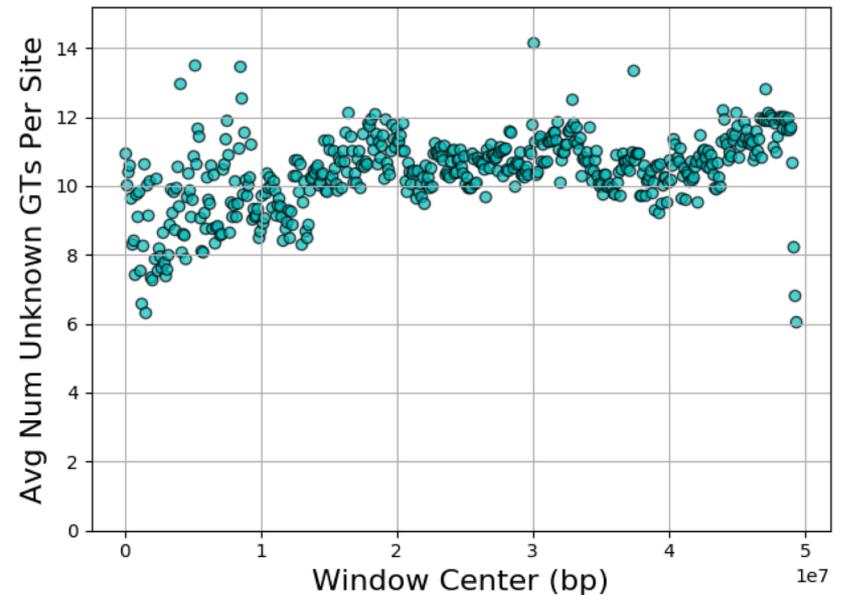
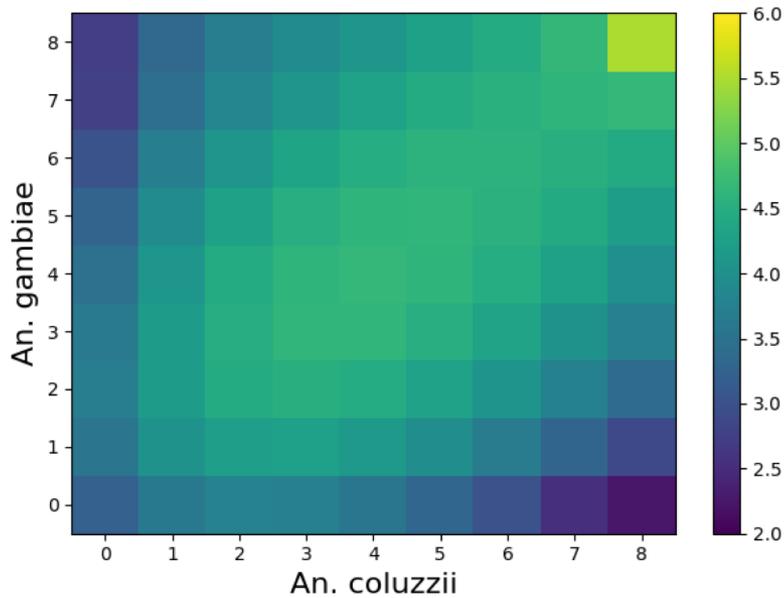
3. Compute G statistic

$$G = 2(\log L(\beta_1, \beta_0 | \mathbf{T}, \mathbf{y}) - \log L(\beta_0 | \mathbf{y})) \quad (3)$$

4. Estimate p-value

$$p = P[\chi^2(df) > G] \quad (4)$$

Unknown Genotypes



Handling Unknown Genotypes

SNP	PC Coordinate
A/A	-3.0
T/T	2.0
X/X	1.75
A/T	0.0

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Likelihood-Ratio Test

1. Fit Logistic Regression model

$$P_g(y_{i,g}) = \frac{1}{1 + \exp(-\beta_1 \mathbf{T}_{i,j} + \beta_0)} \quad (1)$$

2. Compute Likelihoods for Null and Alternative Models

$$L(\beta, \beta_0 | \mathbf{T}, \mathbf{y}) = \prod_{i=1}^N \prod_g P(y_{i,g} | \mathbf{T}_{i,j})^{y_{i,g}/M} \quad (5)$$


3. Compute G statistic

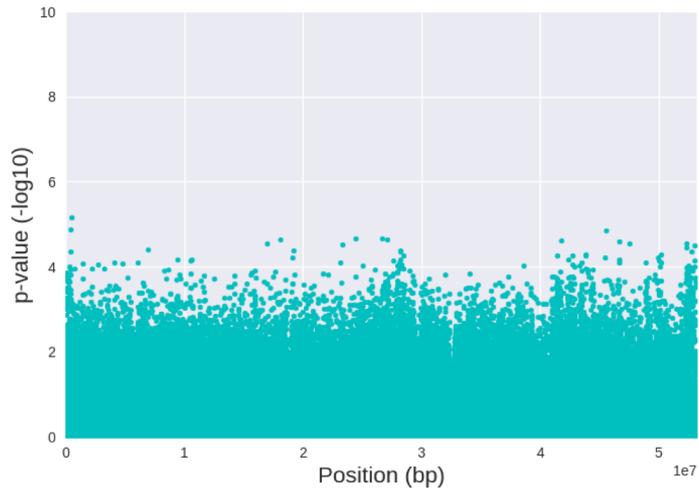
$$G = 2(\log L(\beta_1, \beta_0 | \mathbf{T}, \mathbf{y}) - \log L(\beta_0 | \mathbf{y})) \quad (3)$$

4. Estimate p-value

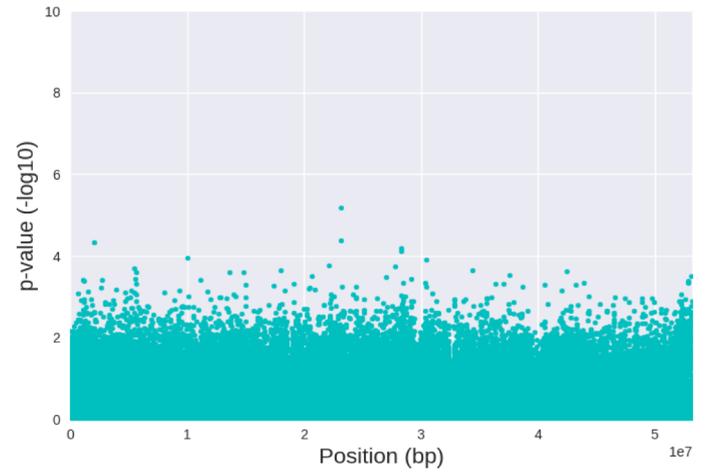
$$p = P[\chi^2(df) > G] \quad (4)$$

No Inversions

Cameroon
3R-PC1

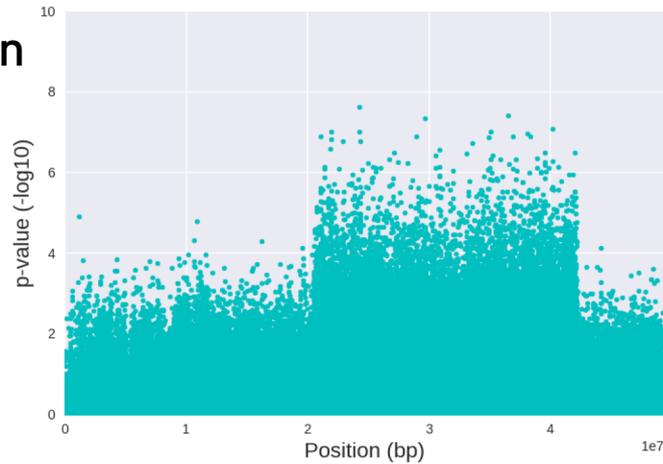


Burkina Faso
3R-PC4

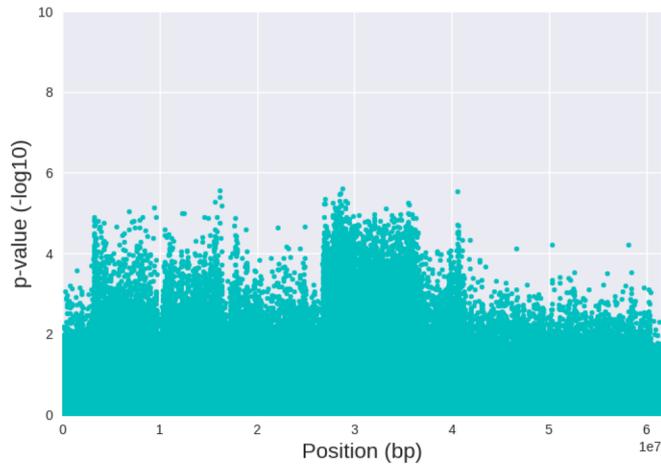


Detecting Inversions

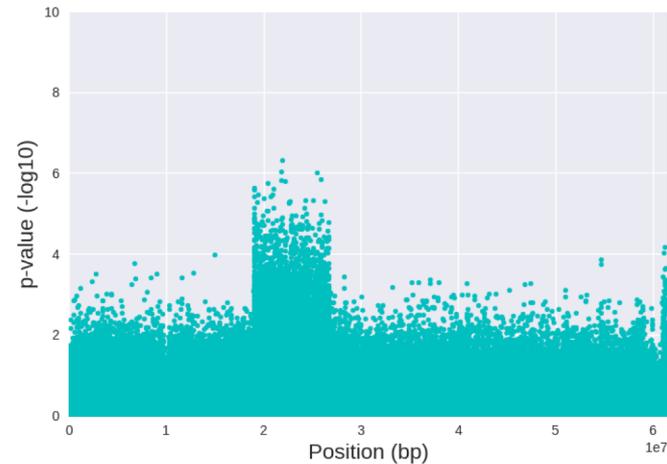
Cameroon
2L-PC1



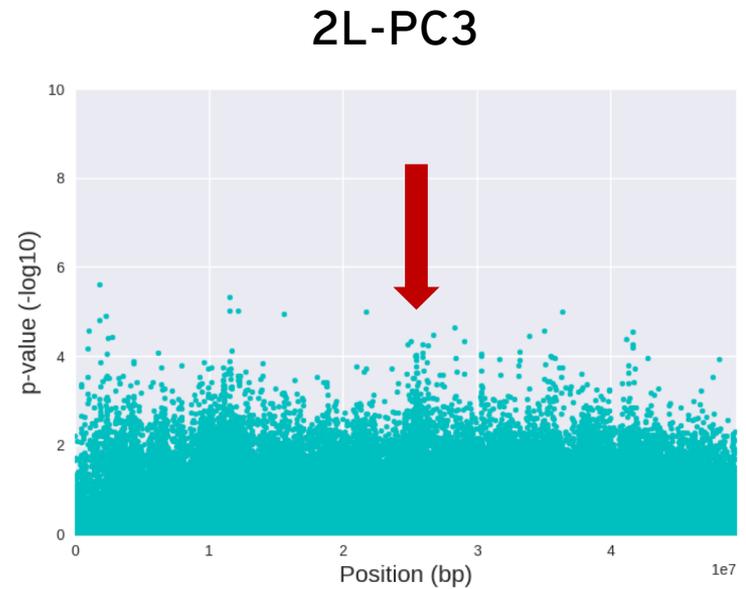
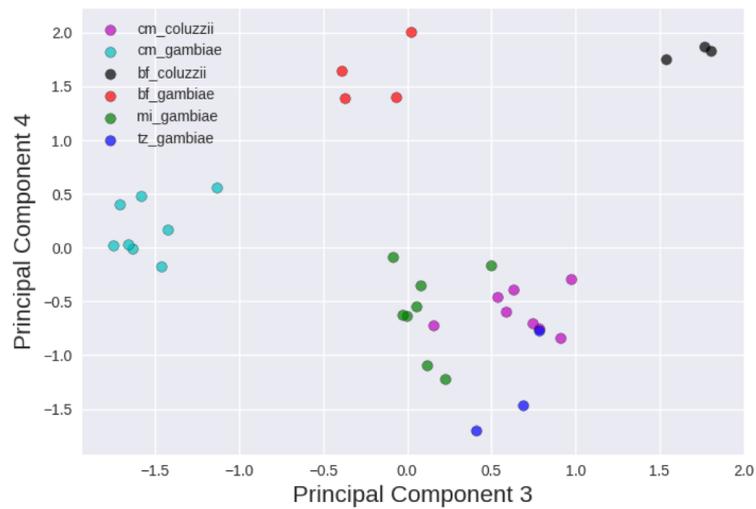
Mali
2R-PC2



Burkina
Faso
2R-PC4

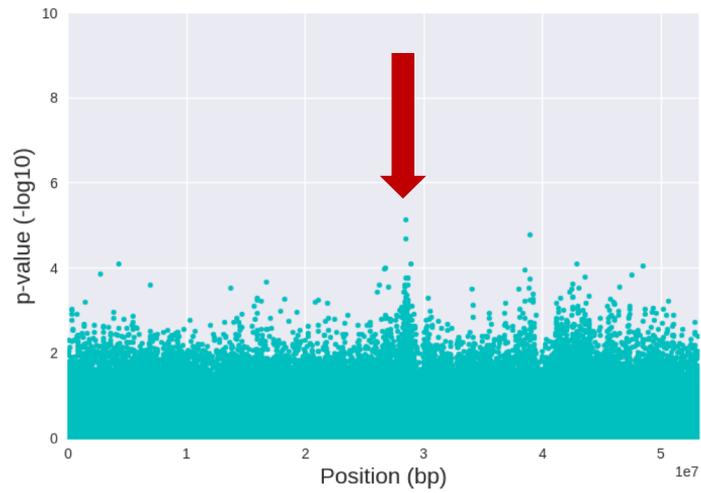


Resistance to Dieldrin (*Rdl*) SNPs

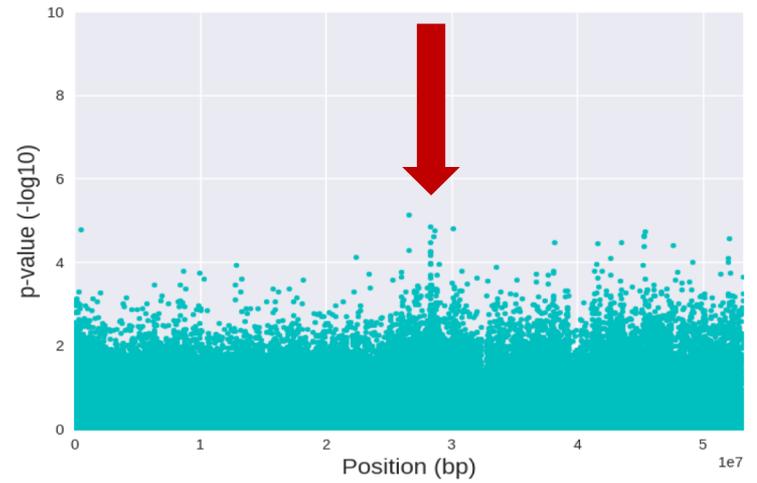


Sweeps

3R-PC3



Mali
3R-PC2



Conclusion

- Inversions of significant biological interest
- PCA of dense SNPs captures inversions but hard to identify from projection plots alone
- Inversion identification enhanced using association tests and Manhattan plots
- Beyond inversions, PCA captures signature of differentiation due to insecticide usage and resistance

Asaph

The screenshot shows the GitHub repository page for 'rnowling/asaph'. The repository is described as a 'SNP analysis package'. It has 263 commits, 2 branches, 0 releases, 1 contributor, and is licensed under Apache-2.0. The page includes navigation tabs for Code, Issues, Pull requests, Projects, Wiki, Insights, and Settings. A file list is shown with columns for file name, description, and commit time.

File Name	Description	Commit Time
asaph	Add density plots to PCA	9 days ago
bin	Initial pass at SNP association tests	11 days ago
tests	Add density plots to PCA	9 days ago
.gitignore	Initial commit	3 years ago
.travis.yml	Make bats tests filter more narrow in .travis.yml	a year ago
Dockerfile	Update Dockerfile to use Debian stretch and thus newer versions of li...	10 days ago
LICENSE	Initial commit	3 years ago
README.md	Fix formatting of file path	5 months ago

<https://github.com/rnowling/asaph>

Questions?

- Acknowledgements

Nora Besansky, Michael Fontaine, Rebecca Love, Aaron Steele, Yue (Shawn) Shen

- Milwaukee School of Engineering is Hiring!

www.msoe.edu